

A pseudoscalar glueball and charmed mesons in the extended Linear Sigma Model *

Walaa I. Eshraim

*Institute for Theoretical Physics,
Johann Wolfgang Goethe University,
Max-von-Laue-Str. 1, D-60438 Frankfurt am Main, Germany*

November 11, 2014

Abstract

In the framework of the so-called extended linear sigma model (eLSM), we include a pseudoscalar glueball with a mass of 2.6 GeV (as predicted by Lattice-QCD simulations) and we compute the two- and three-body decays into scalar and pseudoscalar mesons. This study is relevant for the future PANDA experiment at the FAIR facility. As a second step, we extend the eLSM by including the charm quark according to the global $U(4)_R \times U(4)_L$ chiral symmetry. We compute the masses, weak decay constants and strong decay widths of open charmed mesons. The precise description of the decays of open charmed states is important for the CBM experiment at FAIR.

1 Introduction

The fundamental interactions of quarks and gluons are described by quantum chromodynamics (QCD). The development of an effective hadronic Lagrangian plays an important role in the description of the masses and the interactions of low-lying hadron resonances [1]. To this end, we developed the so-called extended Linear Sigma Model (eLSM) [2] in which (pseudo)scalar and (axial-)vector $q\bar{q}$ mesons and additional scalar and pseudoscalar glueball fields are the basic degrees of freedom. The eLSM emulates the global symmetries of the QCD Lagrangian: the global chiral symmetry (which is exact in the chiral limit), the discrete C, P, and T symmetries, and the classical dilatation (scale) symmetry. When working with colorless hadronic degrees of freedom, the local color symmetry of QCD is automatically preserved. In QCD (and thus also in the eLSM) the global chiral symmetry is explicitly broken by non-vanishing quark masses and quantum effects [4], and spontaneously by a non-vanishing expectation value of the quark condensate in vacuum [5]. The dilatation symmetry is broken explicitly by the logarithmic term of the dilaton potential, by the mass terms, and by the $U(1)_A$ anomaly.

The investigation of the properties of bound states of gluons, so-called glueballs, is an important field of research in hadronic physics. The glueball spectrum has been predicted by Lattice QCD [6], where the third lightest glueball is a pseudoscalar state ($J^{PC} = 0^{-+}$), denoted as $\tilde{G} \equiv gg$, with a mass of about 2.6 GeV, which is studied in the present work.

Studying the properties of the third most massive of all quarks, the charm quark, is an active field of hadronic physics [7]. Thus we extend the eLSM (which has shown success in describing the phenomenology of the nonstrange-strange mesons [2, 8]) from the three quark-flavor case [8] to the four quark-flavor case [9, 10, 11] with only three new unknown parameters related to the charm sector.

*Presented at the 3rd International Conference on New Frontiers in Physics, 28th July - 6th August 2014, Kolymbari, Crete, Greece.

Chiral symmetry is strongly explicitly broken by the current charm quark mass.

In the present work, we compute the two- and three-body decays of the lightest pseudoscalar glueball within the eLSM in the case of three flavors. Moreover, we calculate all meson masses in the eLSM including light and charmed mesons, the (OZI-dominant) strong decays of open charmed mesons, and the weak decay constants of charmed mesons.

These proceedings are organized as follows: in Sec. 2 we present the $U(N_f)_R \times U(N_f)_L$ extended Linear Sigma Model with (axial-)vector mesons. In Sec. 3 we present the vacuum properties of a pseudoscalar glueball within the eLSM. In Sec. 4 we outline the extension of the eLSM to $N_f = 4$ and present the results for the masses, weak decay constants, and decay widths, and in Sec. 5 we provide our conclusions and an outlook.

2 The extended Linear Sigma Model

In this section we present the eLSM Lagrangian which is constructed from two requirements stemming from the underlying QCD theory: (i) global chiral symmetry $U(N_f)_R \times U(N_f)_L$; (ii) dilatation invariance, with the exceptions of the scale anomaly and the $U(1)_A$ anomaly. It is also invariant under the discrete symmetries C and P . The Lagrangian of the eLSM for a generic number of flavors N_f [2, 8, 9, 10, 11, 12] takes the following form

$$\begin{aligned} \mathcal{L} = & \frac{1}{2}(\partial_\mu G)^2 - V_{dil}(G) + \text{Tr}[(D^\mu \Phi)^\dagger (D^\mu \Phi)] - m_0^2 \left(\frac{G}{G_0} \right)^2 \text{Tr}(\Phi^\dagger \Phi) - \lambda_1 [\text{Tr}(\Phi^\dagger \Phi)]^2 \\ & - \lambda_2 \text{Tr}(\Phi^\dagger \Phi)^2 + \text{Tr}[H(\Phi + \Phi^\dagger)] + \text{Tr} \left\{ \left[\left(\frac{G}{G_0} \right)^2 \frac{m_1^2}{2} + \Delta \right] [(L^\mu)^2 + (R^\mu)^2] \right\} \\ & - \frac{1}{4} \text{Tr}[(L^{\mu\nu})^2 + (R^{\mu\nu})^2] - 2 \text{Tr}[E \Phi^\dagger \Phi] + c(\det \Phi - \det \Phi^\dagger)^2 + i c_{\tilde{G}\Phi} \tilde{G}(\det \Phi - \det \Phi^\dagger) \\ & + i \frac{g_2}{2} \{ \text{Tr}(L_{\mu\nu}[L^\mu, L^\nu]) + \text{Tr}(R_{\mu\nu}[R^\mu, R^\nu]) \} + \frac{h_1}{2} \text{Tr}(\Phi^\dagger \Phi) \text{Tr}[(L^\mu)^2 + (R^\mu)^2] \\ & + h_2 \text{Tr}[(\Phi R^\mu)^2 + (L^\mu \Phi)^2] + 2h_3 \text{Tr}(\Phi R_\mu \Phi^\dagger L^\mu) + \dots, \end{aligned} \quad (1)$$

where the field G denotes the dilaton field and its potential [13] reads

$$V_{dil}(G) = \frac{1}{4} \frac{m_G^2}{\Lambda_G^2} \left[G^4 \ln \left(\frac{G}{\Lambda_G} \right) - \frac{G^4}{4} \right], \quad (2)$$

in which the parameter $\Lambda_G \sim N_C \Lambda_{QCD}$ sets the energy scale of the gauge theory. Moreover, $D^\mu \Phi \equiv \partial^\mu \Phi - i g_1 (L^\mu \Phi - \Phi R^\mu)$ is the covariant derivative and contains the (pseudo)scalar quark-antiquark mesons, $L^{\mu\nu} \equiv \partial^\mu L^\nu - \partial^\nu L^\mu$, and $R^{\mu\nu} \equiv \partial^\mu R^\nu - \partial^\nu R^\mu$ are the left-handed and right-handed field strength tensors which describe the (axial-)vector mesons. In eLSM Lagrangian (1) the dots refer to further chirally invariant terms listed in Ref. [8]: These terms do not affect the masses and decay widths studied in the present work and we therefore omitted them. The terms involving the matrices H , E , and Δ are the mass terms and break the dilatation and chiral symmetry due to nonzero current quark masses. Note that the E term is a new term added to the model to account for the charm quark mass, whereas the term $c(\det \Phi - \det \Phi^\dagger)^2$ describes the $U(1)_A$ anomaly. The constant c has dimension $[\text{Energy}]^{4-2N_f}$. Furthermore, the pseudoscalar field is the last field included in the model by the $i c_{\tilde{G}\Phi} \tilde{G}(\det \Phi - \det \Phi^\dagger)$ term (details are provided in the next section).

Spontaneous symmetry breaking takes place when $m_0^2 < 0$ and the scalar-isoscalar fields condense as well as the glueball field $G = G_0$, [2, 8, 9, 10, 11]. To implement this breaking one has to shift the scalar fields $G \rightarrow G_0 + G$ and $\Phi \rightarrow \text{diag}\{\sqrt{2}\sigma_N, \sqrt{2}\sigma_N, \dots\} + \Phi$. Using the eLSM we study the vacuum properties of the lightest pseudoscalar glueball \tilde{G} in the case of $N_f = 3$, and by extending it to $N_f = 4$, we study the phenomenology of charmed mesons. Details will be given in the following two sections.

3 Phenomenology of a pseudoscalar glueball

In this section we compute the decay widths of the pseudoscalar glueball \tilde{G} into a scalar and a pseudoscalar meson, $\tilde{G} \rightarrow PS$ and into three pseudoscalar mesons $\tilde{G} \rightarrow PPP$.

In Ref.[14] we considered an $N_f = 3$ chiral Lagrangian which describes the interaction between the pseudoscalar glueball $\tilde{G} \equiv |gg\rangle$ and (pseudo-)scalar mesons as follows:

$$\mathcal{L}_G^{int} = ic_{\tilde{G}\Phi} \tilde{G} (\det\Phi - \det\Phi^\dagger), \quad (3)$$

where $c_{\tilde{G}\Phi}$ is a dimensionless coupling constant and Φ reads for three flavours, $N_f = 3$ [8]:

$$\Phi = (S^a + iP^a) t^a = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{(\sigma_N + a_0^0) + i(\eta_N + \pi^0)}{\sqrt{2}} & a_0^+ + i\pi^+ & K_S^+ + iK^+ \\ a_0^- + i\pi^- & \frac{(\sigma_N - a_0^0) + i(\eta_N - \pi^0)}{\sqrt{2}} & K_S^0 + iK^0 \\ K_S^- + iK^- & \bar{K}_S^0 + i\bar{K}^0 & \sigma_S + i\eta_S \end{pmatrix}, \quad (4)$$

where S and P refer to scalar and pseudoscalar mesons, respectively, while t^a are generators of the group $U(N_f)$. As discussed in Ref.[14] the multiplet Φ transforms under $U(3)_L \times U(3)_R$ chiral transformations as $\Phi \rightarrow U_L \Phi U_R^\dagger$, whereas $U_{L(R)} = e^{-i\theta_{L(R)}^a t^a}$ is an element of $U(3)_{L(R)}$ and the pseudoscalar glueball \tilde{G} is chirally invariant. We then conclude that the interaction Lagrangian (3) is invariant under $SU(3)_R \times SU(3)_L$ and also invariant under parity ($\Phi \rightarrow \Phi^\dagger$ and $\tilde{G} \rightarrow -\tilde{G}$), but not invariant under the axial $U_A(1)$ transformation.

The states in the interaction Lagrangian are assigned as physical resonances to light quark-antiquark states with mass $\lesssim 2$ GeV [14]. For the pseudoscalar sector P , the fields $\vec{\pi}$ and K represent the pion isotriplet and the kaon isodoublet [8]. The bare fields $\eta_N \equiv |\bar{u}u + \bar{d}d\rangle/\sqrt{2}$ and $\eta_S \equiv |\bar{s}s\rangle$ are the nonstrange and strange contributions of the physical states η and η' which can be obtained by [8]:

$$\eta = \eta_N \cos \varphi + \eta_S \sin \varphi, \quad \eta' = -\eta_N \sin \varphi + \eta_S \cos \varphi, \quad (5)$$

where the mixing angle is $\varphi \simeq 44.6^\circ$ [8]. For the scalar sector S , the field \vec{a}_0 is assigned to the physical isotriplet state $a_0(1450)$ and the scalar kaon fields K_s to the resonance $K_0^*(1430)$. In the scalar-isoscalar sector the bare nonstrange field $\sigma_N \equiv |\bar{u}u + \bar{d}d\rangle/\sqrt{2}$ corresponds to the resonance $f_0(1370)$ [8] but the bare strange field $\sigma_S \equiv |\bar{s}s\rangle$ can be assigned to the resonance $f_0(1710)$ [8] or $f_0(1500)$ [15].

To compute the decays of the pseudoscalar glueball we have to implement the spontaneous symmetry breaking by shifting the scalar-isoscalar fields by their vacuum expectation values as follows [8, 14]:

$$\sigma_N \rightarrow \sigma_N + \phi_N \text{ and } \sigma_S \rightarrow \sigma_S + \phi_S, \quad (6)$$

where ϕ_N and ϕ_S represent the chiral-nonstrange and strange condensates [8], as the following

$$\phi_N = Z_\pi f_\pi, \quad \phi_S = \frac{2Z_K f_K - \phi_N}{\sqrt{2}}. \quad (7)$$

Furthermore, we shift the axial-vector fields and redefine the renormalization constant of the pseudoscalar fields to get rid of the mixing between (axial-)vector and (pseudo)scalar states.

All parameters have been determined in Ref.[8]. Here, we present the theoretical results of the two-body decay $\tilde{G} \rightarrow PS$ and the three-body decay $\tilde{G} \rightarrow PPP$ [14] as branching ratios, where the mass of the pseudoscalar glueball \tilde{G} is 2.6 GeV predicted by Lattice QCD simulation [6] which are independent of the unknown coupling $c_{\tilde{G}\Phi}$ in Table 1. Here, $\Gamma_{\tilde{G}}^{tot} = \Gamma_{\tilde{G} \rightarrow PPP} + \Gamma_{\tilde{G} \rightarrow PS}$ is the total decay width. Note that in the eLSM (3) the decay of the pseudoscalar glueball into three pions vanishes [14]:

$$\Gamma_{\tilde{G} \rightarrow \pi\pi\pi} = 0. \quad (8)$$

Table 1: Branching ratios for the two- and three-body decay of the pseudoscalar glueball \tilde{G} into a scalar and a pseudoscalar meson, where σ_S is assigned either to $f_0(1710)$ or to $f_0(1500)$ (values in parentheses).

Quantity	result in GeV	Quantity	result in GeV
$\Gamma_{\tilde{G} \rightarrow KK_S} / \Gamma_{\tilde{G}}^{tot}$	0.060	$\Gamma_{\tilde{G} \rightarrow KK\eta} / \Gamma_{\tilde{G}}^{tot}$	0.049
$\Gamma_{\tilde{G} \rightarrow a_0\pi} / \Gamma_{\tilde{G}}^{tot}$	0.083	$\Gamma_{\tilde{G} \rightarrow KK\eta'} / \Gamma_{\tilde{G}}^{tot}$	0.019
$\Gamma_{\tilde{G} \rightarrow \eta\sigma_N} / \Gamma_{\tilde{G}}^{tot}$	0.0000026	$\Gamma_{\tilde{G} \rightarrow \eta\eta\eta} / \Gamma_{\tilde{G}}^{tot}$	0.016
$\Gamma_{\tilde{G} \rightarrow \eta'\sigma_N} / \Gamma_{\tilde{G}}^{tot}$	0.039	$\Gamma_{\tilde{G} \rightarrow \eta\eta\eta'} / \Gamma_{\tilde{G}}^{tot}$	0.0017
$\Gamma_{\tilde{G} \rightarrow \eta\sigma_S} / \Gamma_{\tilde{G}}^{tot}$	0.012 (0.015)	$\Gamma_{\tilde{G} \rightarrow \eta\eta'\eta'} / \Gamma_{\tilde{G}}^{tot}$	0.00013
$\Gamma_{\tilde{G} \rightarrow \eta'\sigma_S} / \Gamma_{\tilde{G}}^{tot}$	0 (0.0082)	$\Gamma_{\tilde{G} \rightarrow KK\pi} / \Gamma_{\tilde{G}}^{tot}$	0.47
$\Gamma_{\tilde{G} \rightarrow \eta\pi\pi} / \Gamma_{\tilde{G}}^{tot}$	0.16	$\Gamma_{\tilde{G} \rightarrow \eta'\pi\pi} / \Gamma_{\tilde{G}}^{tot}$	0.095

4 Phenomenology of charmed mesons

In this section we enlarge the eLSM (1) by including the charm quark [9, 10, 11]. We then compute the masses of light and (open and hidden) charmed mesons, the weak decay constants, and the decay widths of open charmed mesons.

In the extension to the four-flavor case, the multiplet Φ as seen in Eq.(4) is extended as follows:

$$\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{(\sigma_N + a_0^0) + i(\eta_N + \pi^0)}{\sqrt{2}} & a_0^+ + i\pi^+ & K_0^{*+} + iK^+ & D_0^{*0} + iD^0 \\ a_0^- + i\pi^- & \frac{(\sigma_N - a_0^0) + i(\eta_N - \pi^0)}{\sqrt{2}} & K_0^{*0} + iK^0 & D_0^{*-} + iD^- \\ K_0^{*-} + iK^- & \bar{K}_0^{*0} + i\bar{K}^0 & \sigma_S + i\eta_S & D_{S0}^{*-} + iD_S^- \\ \bar{D}_0^{*0} + i\bar{D}^0 & D_0^{*+} + iD^+ & D_{S0}^{*+} + iD_S^+ & \chi_{C0} + i\eta_C \end{pmatrix}. \quad (9)$$

The new (pseudo)scalar charmed mesons appear in the fourth line and fourth column. In the pseudoscalar sector there are: an open charmed state $D^{0,\pm}$, open strange-charmed states D_S^{\pm} , and a hidden charmed ground state $\eta_C(1S)$ [9]. In the scalar sector there are open charmed $D_0^{*0,\pm}$ and strange charmed meson $D_{S0}^{*\pm}$ which are assigned to $D_0^*(2400)^{0,\pm}$ and $D_{S0}^*(2317)^{\pm}$ [9], respectively. Similarly, the new (axial-)vector charmed mesons appear also in the fourth line and fourth column of the left- and right-handed matrices which are described as [11]:

$$L^\mu = V_\mu + A^\mu = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{\omega_N + \rho^0}{\sqrt{2}} + \frac{f_{1N} + a_1^0}{\sqrt{2}} & \rho^+ + a_1^+ & K^{*+} + K_1^+ & D^{*0} + D_1^0 \\ \rho^- + a_1^- & \frac{\omega_N - \rho^0}{\sqrt{2}} + \frac{f_{1N} - a_1^0}{\sqrt{2}} & K^{*0} + K_1^0 & D^{*-} + D_1^- \\ K^{*-} + K_1^- & \bar{K}^{*0} + \bar{K}_1^0 & \omega_S + f_{1S} & D_S^{*-} + D_{S1}^- \\ \bar{D}^{*0} + \bar{D}_1^0 & D^{*+} + D_1^+ & D_S^{*+} + D_{S1}^+ & J/\psi + \chi_{C1} \end{pmatrix}^\mu, \quad (10)$$

$$R^\mu = V_\mu - A^\mu = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{\omega_N + \rho^0}{\sqrt{2}} - \frac{f_{1N} + a_1^0}{\sqrt{2}} & \rho^+ - a_1^+ & K^{*+} - K_1^+ & D^{*0} - D_1^0 \\ \rho^- - a_1^- & \frac{\omega_N - \rho^0}{\sqrt{2}} - \frac{f_{1N} - a_1^0}{\sqrt{2}} & K^{*0} - K_1^0 & D^{*-} - D_1^- \\ K^{*-} - K_1^- & \bar{K}^{*0} - \bar{K}_1^0 & \omega_S - f_{1S} & D_S^{*-} - D_{S1}^- \\ \bar{D}^{*0} - \bar{D}_1^0 & D^{*+} - D_1^+ & D_S^{*+} - D_{S1}^+ & J/\psi - \chi_{C1} \end{pmatrix}^\mu. \quad (11)$$

In the vector sector, the nonstrange-charmed fields D^{*0} , $D^{*\pm}$ correspond to $\bar{q}q$ resonances $D^*(2007)^0$ and $D^*(2010)^{\pm}$, respectively, while the strange-charmed $D_0^{*\pm}$ is assigned to the resonance $D_0^{*\pm}$ (with mass $m_{D_0^{*\pm}}$), and there is the lowest vector charmonium state $J/\psi(1S)$. In the axial-vector sector, the open charmed mesons D_1 and D_{S1} are assigned to $D_1(2420)$ and $D_{S1}(2536)$, respectively, whereas the charm-anticharm state χ_{c1} corresponds to the $c\bar{c}$ resonance $\chi_{c1}(1P)$ [9].

In order to implement the spontaneous symmetry breaking we shift the charm-anticharm scalar field χ_{C0} by its vacuum expectation value ϕ_C [9, 10, 11] as

$$\chi_{C0} \rightarrow \chi_{C0} + \phi_C, \quad (12)$$

besides shifting the light scalar-isoscalar fields as seen in Eq. (6). Almost all parameters are determined in the low-energy study of Ref.[8]. We fix the three new parameters related to the charm sector by a fit including twelve masses of hidden and open charmed mesons with $\chi^2/\text{d.o.f} \simeq 1$ (for details see Ref.[9]).

4.1 Masses

In the case of the $U(4)_R \times U(4)_L$ linear sigma model, there are interesting mass differences between vector and axial-vector charmed mesons which depend on the charm condensate ϕ_C , and are independent of the parameters ε_C and δ_C [9]:

$$m_{D_1}^2 - m_{D^*}^2 = \sqrt{2}(g_1^2 - h_3)\phi_N\phi_C, \quad m_{\chi_{C1}}^2 - m_{J/\psi}^2 = 2(g_1^2 - h_3)\phi_C^2, \quad m_{D_{S1}}^2 - m_{D_S^*}^2 = 2(g_1^2 - h_3)\phi_S\phi_C. \quad (13)$$

The theoretical results are

$$m_{D_1}^2 - m_{D^*}^2 = (1.2 \pm 0.6) \times 10^6 \text{ MeV}^2, \quad m_{\chi_{C1}}^2 - m_{J/\psi}^2 = (1.8 \pm 1.3) \times 10^6 \text{ MeV}^2, \\ m_{D_{S1}}^2 - m_{D_S^*}^2 = (1.2 \pm 0.6) \times 10^6 \text{ MeV}^2,$$

while the experimental values are

$$m_{D_1}^2 - m_{D^*}^2 = 1.82 \times 10^6 \text{ MeV}^2, \quad m_{\chi_{C1}}^2 - m_{J/\psi}^2 = 2.73 \times 10^6 \text{ MeV}^2, \quad m_{D_{S1}}^2 - m_{D_S^*}^2 = 1.97 \times 10^6 \text{ MeV}^2.$$

The agreement is fairly good, which shows that our determination of the charm condensate ϕ_C is compatible with experiment, although it still has a large uncertainty.

We obtained the light and charmed meson masses, which are reported in Table 2 [10] and Table 3 [9], respectively. Note that the values of the light meson masses are the same in the case of $N_f = 3$ as shown in the Ref.[8], which are unaffected by the charm sector, because we used the same parameter values as in the case $N_f = 3$.

4.2 Decays

The weak-decay constants of the pseudoscalar open charmed mesons D and D_S [9, 10] are

$$f_D = \frac{\phi_N + \sqrt{2}\phi_C}{\sqrt{2}Z_D} = (254 \pm 17) \text{ MeV}, \quad f_{D_S} = \frac{\phi_S + \phi_C}{Z_{D_S}} = (261 \pm 17) \text{ MeV},$$

where the experimental values [16] are

$$f_D = (206.7 \pm 8.9) \text{ MeV}, \quad f_{D_s} = (260.5 \pm 5.4) \text{ MeV}.$$

We have a good agreement for f_{D_s} and a slightly too large theoretical result for f_D .

The results of (OZI-dominant) strong decay widths of the open charmed mesons described by the resonances D_0^* , D^* , and D_1 are summarized in Table 4 [9, 11].

Table 2: Masses of light meson.

Resonance	J^P	theoretical value [MeV]	experimental value [MeV]
π	0^-	141	139.57018 ± 0.00035
η	0^-	509	547.853 ± 0.024
η'	0^-	962	957.78 ± 0.06
K	0^-	485	493.677 ± 0.016
a_0	0^+	1363	1474 ± 19
σ_1	0^+	1362	$(1200-1500)-i(150-250)$
σ_2	0^+	1531	1720 ± 60
K_0^*	0^+	1449	1425 ± 50
ω_N	1^-	783	782.65 ± 0.12
ω_S	1^-	975	1019.46 ± 0.020
ρ	1^-	783	775.5 ± 38.8
K^*	1^-	885	891.66 ± 0.26
f_{1N}	1^+	1186	1281.8 ± 0.6
a_1	1^+	1185	1230 ± 40
f_{1S}	1^+	1372	1426.4 ± 0.9
K_1	1^+	1281	1272 ± 7

Table 3: Masses of charmed meson

Resonance	J^P	Our Value [MeV]	Experimental Value [MeV]
D^0	0^-	1981 ± 73	1864.86 ± 0.13
D_S^\pm	0^-	2004 ± 74	1968.50 ± 0.32
$\eta_c(1S)$	0^-	2673 ± 118	2983.7 ± 0.7
$D_0^*(2400)^0$	0^+	2414 ± 77	2318 ± 29
$D_{S0}^*(2317)^\pm$	0^+	2467 ± 76	2317.8 ± 0.6
$\chi_{c0}(1P)$	0^+	3144 ± 128	3414.75 ± 0.31
$D^*(2007)^0$	1^-	2168 ± 70	2006.99 ± 0.15
D_s^*	1^-	2203 ± 69	2112.3 ± 0.5
$J/\psi(1S)$	1^-	2947 ± 109	3096.916 ± 0.011
$D_1(2420)^0$	1^+	2429 ± 63	2421.4 ± 0.6
$D_{S1}(2536)^\pm$	1^+	2480 ± 63	2535.12 ± 0.13
$\chi_{c1}(1P)$	1^+	3239 ± 101	3510.66 ± 0.07

Table 4: Decay widths of open charmed mesons

Decay Channel	Theoretical result [MeV]	Experimental result [MeV]
$D_0^*(2400)^0 \rightarrow D\pi$	139^{+243}_{-114}	$\Gamma = 267 \pm 40$
$D_0^*(2400)^+ \rightarrow D\pi$	51^{+182}_{-51}	$\Gamma = 283 \pm 24 \pm 34$
$D^*(2007)^0 \rightarrow D^0\pi^0$	0.025 ± 0.003	seen; < 1.3
$D^*(2007)^0 \rightarrow D^+\pi^-$	0	not seen
$D^*(2010)^+ \rightarrow D^+\pi^0$	$0.018^{+0.002}_{-0.003}$	0.029 ± 0.008
$D^*(2010)^+ \rightarrow D^0\pi^+$	$0.038^{+0.005}_{-0.004}$	0.065 ± 0.017
$D_1(2420)^0 \rightarrow D^*\pi$	65^{+51}_{-37}	27.4 ± 2.5
$D_1(2420)^0 \rightarrow D^0\pi\pi$	0.59 ± 0.02	seen
$D_1(2420)^0 \rightarrow D^+\pi^-\pi^0$	$0.21^{+0.01}_{-0.015}$	seen
$D_1(2420)^0 \rightarrow D^+\pi^-$	0	not seen
$D_1(2420)^+ \rightarrow D^*\pi$	65^{+51}_{-36}	$\Gamma = 25 \pm 6$
$D_1(2420)^+ \rightarrow D^+\pi\pi$	0.56 ± 0.02	seen
$D_1(2420)^+ \rightarrow D^0\pi^0\pi^+$	0.22 ± 0.01	seen
$D_1(2420)^+ \rightarrow D^0\pi^+$	0	not seen

5 Conclusion

In this work we have studied the phenomenology of the pseudoscalar glueball and charmed mesons in an effective model called the extended linear sigma model (eLSM) with vector and axial vector mesons. Firstly we have presented a chirally invariant effective Lagrangian describing the interaction of the pseudoscalar glueball with (pseudo)scalar mesons. We have computed within the eLSM the decay widths of the lightest pseudoscalar glueball into three pseudoscalar and a scalar and pseudoscalar meson. The results are presented as branching ratios which can be measured in the upcoming PANDA experiment at the FAIR facility [17].

Furthermore, the outline of the extension of the eLSM from the three-flavor case to the four-flavor case including the charm quark has been presented. Most parameters are determined in the low-energy study for the nonstrange-strange sector [8]. Three new unknown parameters have been fixed in a fit to the experimental values (details are presented in Ref.[9]). The weak decay constants of nonstrange charm D and strange charm D_S have been calculated. All meson masses in the eLSM (1) have been computed, with the same results for light mesons as in the strange and non-strange sector [8], and with (open and hidden) charmed meson masses being in reasonably good agreement with experimental data [16]. As a last step, we have evaluated the OZI-dominant decays of open charmed mesons (Table 3). The results are compatible with the results and the upper bounds listed by the PDG [16].

Further applications of the described approach are to calculate the decay widths of hidden charmed mesons into light mesons, scalar glueball, and pseudoscalar glueball. This work is currently in progress.

Acknowledgments

The author thanks F. Giacosa and D. H. Rischke for cooperation, and S. Janowski for cooperation in the phenomenology of the pseudoscalar glueball. Financial support from the Deutscher Akademischer Austausch Dienst (DAAD) is acknowledged.

References

- [1] C. Amsler and N.A. Tornqvist, Phys. Rept. **389**, 61 (2004); E. Klemt and A. Zaitsev, Phys. Rept. **454**, 1 (2007) [arXiv: 0708.4016[hep-ph]].

- [2] D. Parganlija, F. Giacosa and D. H. Rischke, Phys. Rev. D **82**, 054024 (2010) [arXiv:1003.4934 [hep-ph]].
- [3] J. S. Schwinger, Annals Phys. **2**, 407 (1957); M. Gell-Mann and M. Levy, Nuovo Cim. **16**, 705 (1960); S. Weinberg, Phys. Rev. Lett. **18**, 188 (1967).
- [4] G. 't Hooft, Phys. Rev. D **14**, 3432 (1976); G. 't Hooft, Phys. Rev. Lett. **37**, 8 (1976); G. 't Hooft, Phys. Rept. **142**, 357 (1986).
- [5] C. Vafa and E. Witten, Nucl. Phys. B **234**, 173 (1984); L. Giusti and S. Necco, JHEP **0704** (2007) 090 [hep-lat/0702013 [HEP-LAT]].
- [6] C. Morningstar and M. J. Peardon, AIP Conf. Proc. **688**, 220 (2004) [arXiv:nucl-th/0309068]; M. Loan, X. Q. Luo and Z. H. Luo, Int. J. Mod. Phys. A **21**, 2905 (2006) [arXiv:hep-lat/0503038]; E. B. Gregory, A. C. Irving, C. C. McNeile, S. Miller and Z. Sroczynski, PoS **LAT2005**, 027 (2006) [arXiv:hep-lat/0510066]; Y. Chen *et al.*, Phys. Rev. D **73**, 014516 (2006) [arXiv:hep-lat/0510074].
- [7] N. Brambilla, A. Pineda, J. Soto and A. Vairo, Rev. Mod. Phys. **77** (2005) 1423.
- [8] D. Parganlija, P. Kovacs, G. Wolf, F. Giacosa and D. H. Rischke, Phys. Rev. D **87**, 014011 (2013) [arXiv:1208.0585 [hep-ph]].
- [9] W. I. Eshraim, F. Giacosa and D. H. Rischke, arXiv:1405.5861 [hep-ph].
- [10] W. I. Eshraim, PoS QCD -**TNT-III**, 049 (2013) [arXiv:1401.3260 [hep-ph]].
- [11] W. I. Eshraim and F. Giacosa, arXiv:1409.5082 [hep-ph].
- [12] F. Giacosa, D. Parganlija, P. Kovacs and G. Wolf, EPJ Web Conf. **37**, 08006 (2012) [arXiv:1208.6202 [hep-ph]].
- [13] A. Salomone, J. Schechter and T. Tudron, Phys. Rev. D **23**, 1143 (1981); H. Gomm and J. Schechter, Phys. Lett. B **158**, 449 (1985); A. A. Migdal and M. A. Shifman, Phys. Lett. B **114**, 445 (1982).
- [14] W. I. Eshraim, S. Janowski, F. Giacosa and D. H. Rischke, Phys. Rev. D **87**, 054036 (2013) [arXiv:1208.6474 [hep-ph]]; W. I. Eshraim, S. Janowski, A. Peters, K. Neuschwander and F. Giacosa, Acta Phys. Polon. Supp. **5**, 1101 (2012) [arXiv:1209.3976 [hep-ph]]; W. I. Eshraim and S. Janowski, PoS ConfinementX **118**, (2012) [arXiv:1301.3345 [hep-ph]]; W. I. Eshraim and S. Janowski, J. Phys. Conf. Ser. **426**, 012018 (2013) [arXiv:1211.7323 [hep-ph]].
- [15] H. Y. Cheng, C. K. Chua and K. F. Liu, Phys. Rev. D **74**, 094005 (2006) [hep-ph/0607206].
- [16] J. Beringer *et al.* (Particle Data Group), Phys. Rev. D **86**, 010001 (2012).
- [17] M. F. M. Lutz *et al.* [PANDA Collaboration], arXiv:0903.3905 [hep-ex].